Name:

Show all of your work and explain your answers fully. There is a total of 100 possible points.

For computational problems, place your answer in the provided boxes. Partial credit is proportional to the quality of your explanation. You may use Sage to form, manipulate and row-reduce matrices. No other use of Sage may be used as justification for your answers. When you use Sage be sure to explain your input and show any relevant output (rather than just describing salient features of something I can't see).

1. Compute the inverse of the matrix B below. Be sure to read the directions above about the use of Sage. (15 points)

	[1	-2	3	-3	
D	1	-1	0	1	
D =	3	-4	4	-4	
	$\lfloor -3 \rfloor$	3	-1	1	



2. Let S the set of four vectors that form the columns of the matrix B in the previous question. Is S linearly independent or not? Cite theorems as part of an explanation of your answer that begins with the fact that A has an inverse and which does not simply quote the NMEx series of results. (15 points)

3. Consider the matrix A below. In each part of this question compute a linearly independent set whose span equals the requested set of vectors, and which meets the extra conditions of each question. (40 points)

$$A = \begin{bmatrix} -39 & -10 & 76 & -93 & 154 & -296 & 365 & 152 \\ -83 & -21 & 162 & -199 & 328 & -631 & 777 & 324 \\ -29 & -7 & 57 & -71 & 115 & -222 & 272 & 114 \\ 5 & 1 & -10 & 13 & -20 & 39 & -47 & -20 \\ 10 & 3 & -19 & 22 & -39 & 74 & -93 & -38 \end{bmatrix}$$

(d) Row space of A,  $\mathcal{R}(A)$ .

(a) Column space of A, C(A). Each vector of your set is a column of A.



(b) Column space of A, C(A). The first few entries of your vectors have a nice "pattern of zeros and ones" which make the linear independence obvious.



(c) Column space of A,  $\mathcal{C}(A)$ . The set is computed using part of the "J" matrix from extended echelon form.

Answer:		

Answer:			

4. For a scalar  $\alpha \in \mathbb{C}$  and an  $m \times n$  matrix A, prove that  $(\alpha A)^t = \alpha A^t$ . Provide justification for each step of your proof in a careful style. (15 points)

5. For a scalar  $\alpha \in \mathbb{C}$ ,  $m \times n$  matrix A and an  $m \times p$  matrix B, prove that  $\alpha(AB) = (\alpha A) B$ . (15 points)